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 Room 220, Lady Shaw Building, The Chinese University of Hong Kong, Shatin, N.T., Hong Kong

# Joint Geometric Analysis Seminar

(Part of MIST program)

## *A Generalization of the Geroch Conjecture with Arbitrary Ends*

*Ms. Shuli Chen  
 Stanford University*

### Abstract

The Geroch conjecture (proven by Schoen-Yau and Gromov-Lawson) states that the torus  $T^n$  does not admit a metric of positive scalar curvature. In this talk, I will explain how to generalize it to some non-compact settings using  $\mu$ -bubbles. In particular, I will talk about why the connected sum of a Schoen-Yau-Schick  $n$ -manifold with an arbitrary  $n$ -manifold does not admit a complete metric of positive scalar curvature for  $3 \leq n \leq 7$ ; this generalizes work of Chodosh and Li. I will also discuss about how to generalize Brendle-Hirsch-Johne's non-existence result for metrics of positive  $m$ -intermediate curvature on  $N^n = M^{n-m} \times T^m$  to manifolds with arbitrary ends for  $n \leq 7$  and certain  $m$ . Here,  $m$ -intermediate curvature is a new notion of curvature interpolating between Ricci and scalar curvature.

Date: February 10, 2023 (Friday)  
 Time: 11:00am-noon (Hong Kong time)  
 ZOOM link: <https://cuhk.zoom.us/j/91805734715>

*All are Welcome*