



# CUHK-SYSU Joint Online Workshop on Geometry and Physics

**Date: July 19, 2021 (Monday)**

**Venue: Online (via ZOOM)**

**Purpose:** Due to the pandemic, it has become very difficult to have international visits nowadays. To facilitate academic communication in mathematics between Sun Yat-sen University (SYSU) and The Chinese University of Hong Kong (CUHK), we organize a series of joint online workshops. This is second workshop in the series, which will be fully supported by CUHK.

**Organizers:**

Kwokwai Chan (CUHK)

Naichung Conan Leung (CUHK)

Changzheng Li (SYSU)

**Schedule:**

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|---------------|---|
| 09:00 – 10:00 | Maurer-Cartan deformation of a Lagrangian<br>by <b>Hansol Hong (Yonsei University)</b>  |
| 10:00 – 11:00 | On Seidel representation of quantum K-theory of Grassmannians<br>by <b>Changzheng Li (Sun Yat-Sen University)</b>               |
| 11:00 – 12:00 | Holomorphic differential operators via Fedosov quantization<br>by <b>Qin Li (Southern University of Science and Technology)</b> |

**Zoom link:**

<https://cuhk.zoom.us/j/91280841007>

Meeting ID: 912 8084 1007

Passcode: 029340

## **Titles and abstracts:**

### **Hansol Hong (Yonsei University)**

Title: Maurer-Cartan deformation of a Lagrangian

Abstract: The Maurer-Cartan algebra of a Lagrangian is the algebra that encodes the deformation of its Floer complex as an  $A_\infty$  algebra. I will give a convenient description of the Maurer-Cartan algebra through a natural homological algebra language, and relate it with (a version of) Koszul duality for the Floer complex. It helps us to obtain the mirror-symmetry interpretation for the Maurer-Cartan deformation and its locality in SYZ situation. Namely, the Maurer-Cartan algebra provides a neighborhood of the point mirror to the Lagrangian, which varies in size depending on geometric types of Floer generators involved in the deformation

### **Changzheng Li (Sun Yat-Sen University)**

Title: On Seidel representation of quantum K-theory of Grassmannians

Abstract: The K-theoretic quantum Pieri rule by Buch and Mihalcea implies a cyclic symmetry on the quantum K-theory of complex Grassmannian  $Gr(k, n)$ . In this talk, we will discuss applications of the Seidel representation. Especially, we will provide an accessible sufficient condition for the reduction of quantum Schubert structure constants of degree  $d$  to that of degree  $d - 1$ . We will also introduce a quantum Littlewood-Richardson rule for  $QK(Gr(3, n))$ . This is my joint work with Chaoyang Liu, Jiayu Song and Mingzhi Yang.

### **Qin Li (Southern University of Science and Technology)**

Title: Holomorphic differential operators via Fedosov quantization

Abstract: Although Toeplitz operators on Kähler manifolds associate smooth function to operators on Hilbert spaces  $\mathcal{H} = H^0(X, L^k)$ , their composition only gives a formal deformation quantization by considering the asymptotic  $k \rightarrow \infty$  and turning  $1/k$  to  $\hbar$ . In this talk, I apply the method of Fedosov to quantize a subclass of smooth functions  $A \subset C^\infty(X)$  to holomorphic differential operators on  $\mathcal{H}_k$ . This gives a strong version of quantization since  $A$  acts on Hilbert spaces as differential operators which gives a non-formal deformation of the classical multiplication.