



Department of Mathematics  
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# Seminar

## *Equilateral triangles in subsets of $\mathbb{R}^d$ of large Hausdorff dimension*

*Mr. Bochen LIU*  
*University of Rochester*

### Abstract

I will discuss how large the Hausdorff dimension of a set  $E \subset \mathbb{R}^d$  needs to be to ensure that it contains vertices of an equilateral triangle. An argument due to Chan, Laba and Pramanik (2013) implies that a Salem set of large Hausdorff dimension contains equilateral triangles. We prove that, without assuming the set is Salem, this result still holds in dimensions four and higher. In  $\mathbb{R}^2$ , there exists a set of Hausdorff dimension 2 containing no equilateral triangle (Maga, 2010).

I will also introduce some interesting parallels between the triangle problem in Euclidean space and its counter-part in vector spaces over finite fields.

It is a joint work with Alex Iosevich.

<b>Date :</b>	October 18, 2016 (Tuesday)
<b>Time :</b>	2:30pm – 3:30pm
<b>Venue :</b>	Room 219, Lady Shaw Building, The Chinese University of Hong Kong

*All are Welcome*