

**THE CHINESE UNIVERSITY OF HONG KONG**  
**Department of Mathematics**  
**MATH3280A Introductory Probability 2024-2025 Term 1**  
**Homework Assignment 1**  
**Due Date: 19 September, 2024 (Thursday)**

I declare that the assignment here submitted is original except for source material explicitly acknowledged, the piece of work, or a part of the piece of work has not been submitted for more than one purpose (i.e. to satisfy the requirements in two different courses) without declaration, and that the submitted soft copy with details listed in the “Submission Details” is identical to the hard copy, if any, which has been submitted. I also acknowledge that I am aware of University policy and regulations on honesty in academic work, and of the disciplinary guidelines and procedures applicable to breaches of such policy and regulations, as contained on the University website <https://www.cuhk.edu.hk/policy/academichonesty/>

It is also understood that assignments without a properly signed declaration by the student concerned will not be graded by the course teacher.

\_\_\_\_\_  
Signature

\_\_\_\_\_  
Date

### General Regulations

- All assignments will be submitted and graded on CUHK Blackboard. You can view your grades and submit regrade requests here as well.
- Late assignments will receive a grade of 0.
- Write your COMPLETE name and student ID number legibly on the cover sheet (otherwise we will not take any responsibility for your assignments). Please write your answers using a black or blue pen, NOT any other color or a pencil.
- Write your solutions on A4 white paper. Please do not use any colored paper and make sure that your written solutions are a suitable size (easily read). Failure to comply with these instructions will result in a 10-point deduction).
- Show all work for full credit. In most cases, a correct answer with no supporting work will NOT receive full credit. What you write down and how you write it are the most important means of your answers getting good marks on this homework. Neatness and organization are also essential.

1. A die is tossed twice. The number of dots facing up in each toss is counted and noted in the order of occurrence.
  - (a) Find the sample space.
  - (b) Find the set  $A$  corresponding to the event *number of dots in first toss is not less than number of dots in second toss*.
  - (c) Find the set  $B$  corresponding to the event *number of dots in first toss is 6*.
  - (d) Does  $A$  imply  $B$  or does  $B$  imply  $A$ ?
  - (e) Find  $A \cap B^c$  and describe this event in words.
  - (f) Let  $C$  correspond to the event *number of dots in dice differs by 2*. Find  $A \cap C$ .
2. Suppose that  $A$  and  $B$  are mutually exclusive events for which  $P(A) = .35$  and  $P(B) = .54$ . What is the probability that
  - (a) either  $A$  or  $B$  occurs?
  - (b)  $A$  occurs but  $B$  does not?
  - (c) both  $A$  and  $B$  occur?
3. A total of 28 percent of Hong Kong males smoke cigarettes, 8 percent smoke cigars, and 6 percent smoke both cigars and cigarettes.
  - (a) What percentage of males smokes neither cigars nor cigarettes?
  - (b) What percentage of males smokes cigars but not cigarettes?
4. Five people, designated as Adin, Bob, Carl, Dan, and Eddy, are arranged in linear order. Assume that each possible order is equally likely. What is the probability that
  - (a) there is exactly one person between Adin and Bob?
  - (b) there are exactly two people between Adin and Bob?
  - (c) there are exactly three people between Adin and Bob?
5. At a certain university, three professors, Mary, Peter, and David, are nominated for an award. Let  $A$ ,  $B$ , and  $C$  denote the events, respectively, that these professors will be given awards. Find an expression in terms of  $A$ ,  $B$ ,  $C$  for the event that the award goes to
  - (a) only Mary;
  - (b) at least one of the three;
  - (c) none of the three;
  - (d) exactly two of them;
  - (e) exactly one of them;
  - (f) Mary or Peter but not both.

6. Let  $A$  and  $B$  be two events. Prove that

$$P(A \cap B) \geq P(A) + P(B) - 1.$$

7. Let  $A$ ,  $B$ , and  $C$  be three events. Show that exactly two of these events will occur with probability

$$P(A \cap B) + P(A \cap C) + P(B \cap C) - 3P(A \cap B \cap C).$$