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Joint Geometric Analysis Seminar

Pseudo-convex submanifolds — curvature properties, Plateau problem, and the discrete theory

Prof. Xiang Ma
Peking University

Abstract:

As a generalization of the usual convex hypersurfaces, we consider a spacelike submanifold immersed in a pseudo Euclidean space, whose normal bundle is induced with a Lorentz inner product of signature $(1,p)$, and we make a convexity assumption on its second fundamental form. The simplest example is a closed curve in the 3-dimensional Lorentz space whose tangent and normal vectors span a spacelike plane, and it winds around some timelike axis with index 1. For such a pseudo-convex loop, we show that it satisfies a reversed Fenchel type inequality (its total curvature is no more than 2π), and it always span a spacelike maximal surface. Then we give the general definition of a pseudo-convex submanifold and demonstrate their close relationship with convex hypersurfaces. If time is allowed we will briefly mention what is a pseudo-convex polyhedron and a discretized Positive Mass Conjecture about the Liu-Yau mass. This is a joint work with Dr. Nan Ye, and the final part is an ongoing project with my postdoc Dong Zhang.

Date: 1 February 2018 (Thursday)
Time: 10:30 a.m. – 11:30 a.m.
Venue: Room 502A, Academic Building No.1
The Chinese University of Hong Kong, Shatin

All are Welcome!